

TUES.

1-8-08

P. 34 II

$$\textcircled{1} \left\{ \frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6} \right\} \quad \textcircled{3} \left\{ 0, \pi, \frac{\pi}{3}, \frac{5\pi}{3} \right\}$$

$$\textcircled{5} \left\{ 0, \pi, \frac{\pi}{6}, \frac{5\pi}{6} \right\} \quad \textcircled{7} \left\{ \frac{2\pi}{6}, \frac{11\pi}{6}, \pi \right\}$$

$$\textcircled{9} \left\{ \frac{\pi}{6}, \frac{5\pi}{6}, \frac{3\pi}{2} \right\} \quad \textcircled{11} \left\{ \frac{\pi}{6}, \frac{5\pi}{6} \right\}$$

$$\textcircled{8} \left\{ \frac{\pi}{2} \right\}$$

GENERAL SOLUTIONS

$$\textcircled{3} \left\{ x: x = k\pi \cup x = \frac{\pi}{3} + 2k\pi \cup x = \frac{5\pi}{3} + 2k\pi \right\}$$

$$\textcircled{9} \left\{ x: x = \frac{\pi}{6} + 2k\pi \cup x = \frac{5\pi}{6} + 2k\pi \cup x = \frac{3\pi}{2} + 2k\pi \right\}$$

$$\sin 2x + \sin x \stackrel{?}{=} \sin x \quad ?$$

2

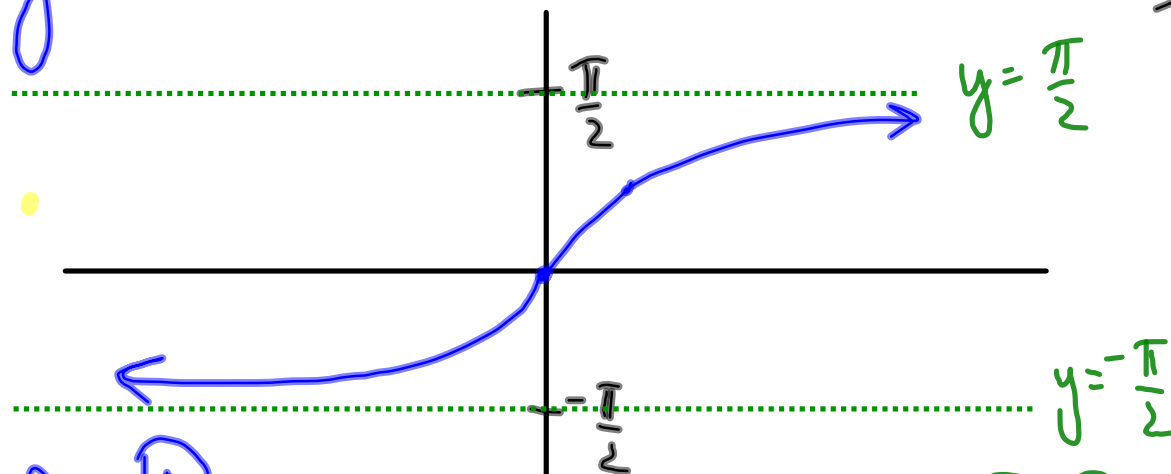
OK:  $2\sin x - \sin x = \sin x$

$$\sin 2x - \sin x \stackrel{?}{=} \sin x (\sin x - 1) ?$$

OK:  $\sin 2x - \sin x = 2\sin x \cos x - \sin x$   
 $= \sin x (2\cos x - 1)$

OK:  $\sin^2 x - \sin x = \sin x (\sin x - 1)$

$$y = \tan^{-1} x \equiv \text{Arctan } x$$



- $D = \mathbb{R}$
- $R = \left\{ y : y \in \mathbb{R}, -\frac{\pi}{2} < y < \frac{\pi}{2} \right\}$

$$\tan^{-1} \sqrt{3} = ?$$

$$\underline{\underline{\frac{\pi}{3}}}$$

$$\text{Arctan}(-\sqrt{3}) = ?$$

$$\underline{\underline{-\frac{\pi}{3}}}$$

Ex) SOLVE:  $x = 4$

$$x^2 = 16$$

$$x^2 - 16 = 0$$

$$(x-4)(x+4) = 0$$

$$x-4=0 \text{ or } x+4=0$$

$$x=4 \text{ or } x=-4$$

~~{4, -4}~~

EXTRANEIOUS  
ROOT

\*LAST RESORT

4

WHEN YOU SQUARE BOTH SIDES  
OF AN EQUATION, YOU MUST  
CHECK ALL SOLUTIONS IN THE  
ORIGINAL & DISCARD ONES  
THAT DON'T WORK IN THE  
ORIGINAL EQUATION.

Ex) SOLVE:  $0 \leq x < 2\pi$ :  $\cos x = 1 + \sqrt{3} \cdot \sin x$  5

① ISOLATE THE  $\sqrt{\quad}$  TERM:  $\cos x - 1 = \sqrt{3} \cdot \sin x$

② SQUARE BOTH SIDES:  $(\cos x - 1)^2 = (\sqrt{3} \cdot \sin x)^2$

$$(\cos x - 1)(\cos x - 1) = \sqrt{3} \cdot \sin x \cdot \sqrt{3} \cdot \sin x$$

$$\cos^2 x - 2\cos x + 1 = 3 \cdot \sin^2 x$$

$$\cos^2 x - 2\cos x + 1 = 3(1 - \cos^2 x)$$

$$\cos^2 x - 2\cos x + 1 = 3 - 3\cos^2 x$$

$$4\cos^2 x - 2\cos x - 2 = 0 \text{ NEXT PAGE...}$$

$$4\cos^2 x - 2\cos x - 2 = 0$$

$$2(2\cos^2 x - \cos x - 1) = 0$$

$$2(2\cos x + 1)(\cos x - 1) = 0$$

$$2 = 0 \text{ OR } 2\cos x + 1 = 0 \text{ OR } \cos x - 1 = 0$$

Silly

$$2\cos x = -1$$

$$\cos x = 1$$

$$\cos x = -\frac{1}{2}$$

$$x = \frac{2\pi}{3}, \frac{4\pi}{3}$$

$$x = 0$$

\* CHECK IN ORIGINAL!

$$\left\{ 0, \frac{4\pi}{3} \right\}$$

1.1	1.2	1.3	RAD	AUTO	REAL
$\cos(x) _{x=0}$					1
$1+\sqrt{3}\cdot\sin(x) _{x=0}$					1
$\cos(x) _{x=\frac{2\cdot\pi}{3}}$					$-\frac{1}{2}$
$1+\sqrt{3}\cdot\sin(x) _{x=\frac{2\cdot\pi}{3}}$					$\frac{5}{2}$

NO

DISCARD

1.1	1.2	1.3	RAD	AUTO	REAL
$1+\sqrt{3}\cdot\sin(x) _{x=\frac{2\cdot\pi}{3}}$					$\frac{5}{2}$
$\cos(x) _{x=\frac{4\cdot\pi}{3}}$					$-\frac{1}{2}$
$1+\sqrt{3}\cdot\sin(x) _{x=\frac{4\cdot\pi}{3}}$					$-\frac{1}{2}$

P.35 CORRECTIONS:

3 f) ~~into~~ → into

4) SOLVE TO THE NEAREST THOUSANDTH  
GRAPHICALLY BY ~~ZOOMING IN~~

4 c) FIND THE OTHER POINTS  
OF INTERSECTION. ~~WITHOUT...~~ <sup>(CALC) (INTERSECT)</sup>

O.T.L. · CORRECT TODAY'S O.T.L.  
(TURN IN PERFECT!)

· P.34 II 13

· P.35 4, 8, 9 a, c, e, ...

$$\textcircled{8} \quad 3\csc x - \sin x = 2$$

$$\sin x \left[ \frac{3}{\sin x} - \sin x = 2 \right]$$

$$3 - \sin^2 x = 2 \sin x$$

$$0 = \sin^2 x + 2 \sin x - 3$$

⋮

8



$$\textcircled{5} \quad \underbrace{\cos 2x + \sin x - 1 = 0}$$
$$1 - 2\sin^2 x + \sin x - 1 = 0$$

⋮

$$\textcircled{11} \quad \tan x = \frac{1}{2} \sec x$$

$$2\cos x \left[ \frac{\sin x}{\cos x} = \frac{1}{2} \cdot \frac{1}{\cos x} \right]$$

$$2\sin x = 1$$

⋮

$$\textcircled{9} \quad \cos 2x = \sin x$$

$$1 - 2\sin^2 x = \sin x$$

$$0 = 2\sin^2 x + \sin x - 1$$

⋮